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DH'17

Proceedings of the 2017 International Conference on **Digital Health**

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Welcome to Digital Health 2017

Welcome to the 7th International Conference on Digital Health (www.acm-digitalhealth.org), supported by UCL Institute for Risk and Disaster Reduction and held in-cooperation with ACM Special Interest Group on Knowledge Discovery and Data Mining (SIGKDD) in London, UK on 2-5 July, 2017.

Building on the growing success of previous editions (ehealth 2008 in London, 2009 in Istanbul, 2010 in Casablanca and ehealth 2011 in Malaga) and two editions of the International Workshop on Public Health in the Digital Age (1st PHDA 20113 and 2nd PHDA 2014), the 5th and 6th Digital Health conference was colocated with the World Wide Web conference in 2015 in Florence and in 2016 in Montreal. Digital Health has become a prime interdisciplinary international venue proudly bringing together frontline public health professionals, global health experts and computer science researchers in data mining, crowdsourcing and Big Data analysis for public health surveillance. Following the successful publication strategy, DH 2017 proceedings are included in the ACM Digital Library.

This year DH 2017 is a standalone event in London, sponsored by the UCL Institute for Risk and Disaster Reduction. The move has worked out superbly - DH 2017 attracted the highest number of paper submissions, ensuring growing scientific quality of the event and growing interest from NGOs, industry, start-up innovators and charitable sector. As we also expanded the remit to cover digital solutions for emergencies and humanitarian health, the seventh DH 2017 promises to deliver the highest quality and diversity programme since its foundation.

We are excited about the great keynotes in store this year, including Dr Oliver Morgan from the WHO who will deliver a talk on public health emergencies and data to save lives, Dr Tina Comes of the University of Delft speaking about designing Humanitarian Technology and Dr Paul Chong of IBM Watson discussing a joint project with Alder Hey Children's NHS Foundation Trust - the 'cognitive hospital'. Three strategic panels chaired by leading international experts in the domain will discuss the role of funding (chaired by Prof Michael Arthur, UCL provost), the future of digital imaging and microscopy (chaired by Dr Isaac Bogoch) and the role of data sharing for emergencies (chaired by Dr Michael Edelstein).

We have a great academic programme including 13 full papers, 18 short papers, 6 extended medical abstracts, 29 posters and 7 demonstrators, and 11 abstracts from PhD students – plus a confirmed line-up of industry and healthcare speakers. We have also introduced a bespoke session for the SME and start-up sector bringing world class innovators together to discuss the path to success, challenges and lessons learned to inspire the new generation of innovators. The Digital Health Innovation Award – offering recognition to companies in several categories - was launched in collaboration with the Digital Catapult, UK.

For more up-to-date information, 'follow' and 'like' DH 2017 on social media:

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Finally, we would like to thank everyone who contributed to the 7th International Conference in Digital Health 2017, ensuring the event will be an overwhelming success: authors of the submitted papers, posters and demos, speakers, the Senior Programme Committee members and Programme Committee members, Organising Committee chairs, session chairs and above all the back office team at UCL IRDR for making such a large event a reality.

Patty Kostkova, Floriana Grasso, Carlos Castillo, Yelena Mejova, Arnold Bosman May 2017

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On Consolidated Predictive Model of the Natural History of Breast Cancer: Primary Tumor and Secondary Metastases in Patients with Lymph Nodes Metastases

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ABSTRACT

This paper is devoted to mathematical modelling of the progression and stages of breast cancer. The âĂIJConsolidated mathematical growth Model of primary tumor (PT) and secondary distant metastases (MTS) in patients with lymph nodes MTS (Stage III)" (CoM-III) is proposed as a new research tool. The CoM-III rests on an exponential tumor growth model and consists of a system of determinate nonlinear and linear equations. The CoM-III describes correctly primary tumor growth (parameter T) and distant metastases growth (parameter M, parameter N). The CoM-III model and predictive software: a) detect different growth periods of primary tumor and distant metastases in patients with lymph nodes MTS; b) make forecast of the period of the distant metastases appearance in patients with lymph nodes MTS; c) have higher average prediction accuracy than the other tools; d) can improve forecasts on survival of breast cancer and facilitate optimisation of diagnostic tests. The CoM-III enables us, for the first time, to predict the whole natural history of PT and secondary distant MTS growth of patients with/without lymph nodes MTS on each stage relying only on PT sizes.

CCS CONCEPTS

• Applied computing \rightarrow Consumer health; Health informatics; • Mathematics of computing \rightarrow Solvers;

KEYWORDS

breast cancer; mathematical modelling; exponential model; primary tumor; secondary metastases; lymph nodes metastases; survival; predictor

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1 INTRODUCTION

Breast Cancer (BC) is the most common cancer and also the leading cause of cancer mortality in women worldwide. BC accounts for about 20-25% of all cancer types in women [21].

Finding algorithms to predict the growth of tumors has piqued the interest of researchers ever since the early days of cancer research. Many studies were carried out as an attempt to obtain reliable data on the natural history of BC growth.

Mathematical modeling can play a very important role in the prognosis of BC. Various mathematical models were built to describe primary tumor (PT) growth and distant metastases (MTS) growth separately [19].

These days, an exponential, Gompertz, logistic and von Bertalanffy models are included in a group of classical mathematical models of PT growth [1]. For the breast data, the observed linear dynamics were best captured by an exponential model, which is situated for the description of PT growth and, also, for secondary distant MTS growth [7, 8, 10–16, 18]. As for Gompertz and logistic models, they are used rarely in order to describe PT growth or secondary distant MTS growth [5, 9, 17, 25].

The duration of the period from the first BC cell to death refers to the natural history of BC [2]. Secondary distant MTS appear in various time in different organs. The interval between removal of PT and the first clinical manifestation of MTS (MTS free survival time or non-visible period) determined by PT size, the number of affected lymph nodes and MTS growth rate [3, 5, 7–10, 12–16, 18, 22, 25, 26]. Survival (lifetime) is the period between the date of diagnosis (TNM staging system of BC) and the date of a patient death [21]. Survival among BC patients (%) indicates the percentage of people in a study or treatment group who are alive for a given period of time after diagnosis. The percentage of patients who live at least 5-, 10-, 15-, 20-, 25- and 30-years after being treated PT is defined as 5-, 10-, 15-, 20-, 25- and 30-years observed survival rate of BC patients [9, 21].

It is important to highlight that the natural history of BC continues after removal of PT. The next stage begins with secondary distant MTS manifestation. When the MTS reach the threshold volume, patients die from progression of BC [1, 4, 7–10, 12–16, 18, 20, 22]. All BC patients get a comprehensive treatment of PT, so the *whole natural history of BC* should include the period of secondary distant MTS growth (Fig. 1):

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- 1) the **non-visible** period of PT growth;
- the visible period of PT growth, diagnostics and removal of PT;
- 3) the non-visible period of secondary distant MTS growth;
- the visible period of secondary distant MTS growth, diagnostics, treatment and patient's death.



Figure 1: Scheme of the *whole natural history* **of BC (stage I-II)[4, 7, 12, 14, 20, 22].** As it should be highlighted, the main feature is that model describes PT growth and secondary distant MTS growth as a whole (as indivisible dependent process). Ordinate (Y): Diameter of tumor (mm). Abscissa (X): Time (years).

Legend of Fig.	1:	
t_{1tmr}	_	date of appearance of the first BC stem cell;
$t_{1tmr5mm}$	_	date of appearance of the visible PT with size 5 mm:
t _{lethal1tumor}	-	date of appearance of the lethal PT with size 100 mm (when PT reaches the thresh-
t _{1mts}	_	old volume); date of appearance of the first MTS stem cell, which coincides with the period of 20 th doubling time;
$t_{1mts5mm}$	-	date of appearance the first visible MTS of breast cancer with size 5 mm;
t _{lethal1mts}	-	date of appearance the first lethal MTS of BC with size 100 mm (when secondary dis- tant MTS reaches the threshold volume);
t _{Xmts}	-	date of appearance nXmts cell of BC MTS, which coincides with date of surgery;
t _{Xmts5mm}	—	date of appearance nXmts visible BC MTS with size 5 mm;
t _{lethalXmts}	_	date of appearance nXmts lethal BC MTS with size 100 mm;
US_1	_	date and sizes of the first US of PT;
US_2	_	date and sizes of the second US of PT.
Given the rela	tion	between PT and MTS the problem of dis

Given the relation between P1 and M1S, the problem of discovering BC process seems to be twofold: firstly, it is important to describe the *whole natural history of BC* to understand the process as a whole; secondly, it is necessary to predict the period of a clinical MTS manifestation. Yet, the papers available for this do not offer mathematical growth models of MTS that relate to TNM classification. That leads to the demand building a mathematical model that rests on an exponential classical mathematical model and describes *whole natural history of BC* and corresponds to TNM classification. Moreover, the latter aspect of the problem is reflected only by statistical tools that are available as open source. In other words, a patient provides diagnostic data to predictor, and the tool calculates MTS free period and survival according to statistical data. Consequently, it is necessary to create a predictor that makes prognosis of BC for a patient independently from statistical data, and requires no expensive diagnostic data. Thus, this research possesses a novelty since it is the first time the following tools for BC have been proposed: a) *whole natural history of BC*; b) mathematical growth model corresponding to TNM; c) non statistical software tool for prediction of BC developing.

To avoid terminological ambiguities, we dwell upon recalling some standard terms and TNM staging system of BC (Table 1) [21].

Table 1: TNM staging system

Stage Parameter T		Parameter T	Parameter N	Parameter M	
	Ι	T1	N0	M0	
	II	T1, T2	N0, N1	M0	
	III	T1, T2, T3, T4	N1, N2, N3	M0	
	IV	any T	any N	M1	

Legend of Table 1:

parameter T	_	size of PT: T1 = 0.1 d \leq 2 cm; T2 = 2 d \leq 5
		cm; $T3 = d > 5$ cm; $T4 = spread$;
parameter N	_	the number of affected lymph nodes: N0: n
		= 0; N1: n = 1-3; N2: n = 4-9; N3: n = 10-18;
parameter M	_	existence of distant MTS (lungs, bones,
		liver, etc): M0 = MTS not exist; M1 = MTS
		exist.
T1	d	

The **goal** of the research is to improve the prediction accuracy of BC process using the original **Consolidated** mathematical growth **M**odel of primary tumor and secondary MTS of patients with lymph nodes MTS (CoM-III). To make precise the scope of the study it is necessary to fulfil several **tasks**:

- modelling the *whole natural history* of PT and MTS for stage III;
- (2) developing the adequate and precise CoM-III that reflects relations between PT and secondary MTS of patients with lymph nodes MTS;
- (3) analysing the CoM-III scope of applications;
- (4) implementing the model as a software tool.

Practical value. As it turns out, a new software tool for prediction of BC developing can calculate more accurately: a) MTS free period; b) survival for stage III of BC including PT and secondary MTS of patients with lymph nodes MTS. Moreover, the predictor can estimate a quality of treatment which was prescribed to a patient. Summarising: the CoM-III describes correctly PT and secondary distant MTS growth of T1N1M0, T2N1M0, T1-2N2M0, T3N1-2M0, T4N1-2M0, T1-4N3M0 [T1-4N1-3M0] stages in patients with lymph nodes MTS (N1-3).

2 MATERIALS AND METHODS

Consolidated mathematical growth model of PT and secondary MTS, I-II stages (CoMPaS)

In 2015 we proposed a consolidated mathematical growth model of PT and secondary MTS (CoMPaS) that describes correctly PT growth (parameter T) as well as secondary MTS growth (parameter M), corresponds to TMN [23]. Also, the CoMPaS might facilitate the survival (lifetime) and, as a consequence, make predictions of a future metastatic manifestation after removal of PT.

It is important to define several admissions, where rows 1-3 rests on [1, 7, 8, 10-15, 18, 20, 22, 24]:

- an exponential growth model is used widely for description *natural* growth rate of the primary BC;
- the *natural* rate of secondary distant MTS is the same as *natural* growth rate of the primary BC;
- the period of appearance of the first metastatic cell of secondary distant MTS coincides with the 20th doubling of the primary BC. It allows us to define the **non-visible** growth period of MTS and the initial period of **non-visible** MTS manifestation;
- 4) the *whole nature history* of the PT and secondary distant



Figure 2:	The first MTS	cell appears	on the 20 th	doubling	of PT
i igui e bi	The mot wite	cen appears		acabing	OL L L

1.00.0

Legend of Fig. 2:	
red points	correspond to PT growth;
blue points	correspond to distant MTS growth;
the non-visible period	of MTS growth starts with a removal of
	PT;
red horizontal block	indicates a minimal size of tumor that can
	be diagnosed [1mm; 5mm];
growth rate	is equal as for PT as for MTS (CoMPaS for
	Stages I-II);
three vertical lines	on the left side of the Fig. 2 show the num-
	ber of cells in tumor with corresponding
	diameter;
60 th doubling	means the death of a patient;
\xrightarrow{time}	illustrates a mean survival at corresponded
	acapining.

The CoMPaS rests on an exponential growth model and consisted of nonlinear and linear determined equations [1, 3, 5, 7, 8, 10-16, 18, 20, 22, 24, 26]:

$$\begin{aligned} \frac{dV}{dt} &= \frac{\log 2}{DT} V, \ t \leq DT \ \log_2\left(\frac{\theta \ DT}{\log 2} \ V_0\right); \\ \frac{dV}{dt} &= \theta \log V, \ t > DT \ \log_2\left(\frac{\theta \ DT}{\log 2} \ V_0\right); \\ V(t=0) &= V_0 \end{aligned}$$
$$Survival &= PT_{\log(V)} + Nonvis_{log} + Vis_{log} = 60; \\ TVDT_{non} &= TVDT_{vis} = \frac{NonVis_{days} + Vis_{days}}{NonVis_{log} + Vis_{log}}; \end{aligned}$$

_	the fraction of proliferative cells times;
_	drives the linear phase;
_	the number of PT doublings;
_	the number of doublings for non-visible
	growth period of MTS;
_	the number of doublings for visible
	growth period of MTS;
_	tumor volume doubling time;
_	the whole nature growth history of the PT
	and secondary distant MTS.

According to M. Schwartz (1961): "the doubling time (DT), representing the time for 1 cell (or of the tumor as a whole if each cell has the same doubling time) to double in volume, and it is equivalent to the interval between successive mitoses" [20]:

$$DT = \frac{\log 2 (t_1 - t_0)}{\log V_1 - \log V_0},$$

the period of doubling time;

- tumor volume at time *t* of the pre-surgery measurement;
- tumor volume at time of the first measurement;
- $t_1 t_0$ the period between the first and presurgery measurements (days).

3 RESULTS

DT

 V_1

 V_0

Consolidated mathematical growth model of PT and secondary MTS of patients with lymph nodes MTS, III stage (CoM-III)

Stage III (T1-4N1-3M0) means that lymph nodes MTS (N1-3) exist meanwhile PT (T1-4) is growing [6, 21]. Moreover, patients with lymph nodes MTS have lower survival comparing with patients without lymph nodes MTS. Unfortunately, the papers available for this do not offer mathematical growth models of stage III of BC that cover growth process of PT and secondary MTS in patients with lymph nodes MTS.

We propose a new mathematical growth model for PT and secondary MTS in patients with lymph nodes MTS. The model may help to improve predicting accuracy of BC process using an original mathematical model referred to CoM-III and corresponding software. Consequently, we are interested in:

- modelling the *whole natural history* of PT and secondary MTS in patients with lymph nodes MTS;
- developing adequate and precise CoM-III that reflects relations between PT and MTS;
- analysing the CoM-III scope of application; 4) implementing the model as a software tool.

The period of appearance of the first metastatic cell coincides with 20th doubling of PT. At stage III the period of MTS manifestation depends on the number of lymph nodes MTS.

The CoM-III rests upon CoMPaS, and by complementing formulas::

$$\begin{cases} sMts_{\log(V)(N+)} = pI_{\log(V)} - 20; \\ K_{sMts(N+)} = \frac{20}{sMts_{\log(V)(N+)} \times 18 \times n} + 1; \\ TVDT_{sMts(N+)} = \frac{TVDT_{pT}}{K_{sMts(N+)}}; \end{cases}$$

the number of doublings of secondary $sMts_{\log(V)(N+)}$ MTS in patients with lymph nodes MTS; $pT_{\log(V)}$ the number of doublings of PT; the number of doublings of PT that co-20 incides with the appearance of the first metastatic cell; correcting coefficient of secondary MTS of $K_{sMts(N+)}$ patients with lymph nodes MTS relating with PT growth rate; the number of affected lymph nodes (min n $= 0, \max = 18);$

$$TVDT_{sMts(N+)}$$
 – tumor volume doubling time of secondary
MTS of patients with lymph nodes MTS
relating with tumor volume doubling time
of the PT ($TVDT_{pT}$).

It allows us to calculate different growth periods of PT and secondary MTS of patients with lymph nodes MTS:

- 1) **non-visible** period for PT;
- non-visible period for secondary MTS of patients with lymph nodes MTS;
- 3) **visible** period for secondary MTS of patients with lymph nodes MTS.

Predictor CoM-III

At this stage, it is relevant to shed light on predictor specifications. We implement the CoM-III as a software tool. The application is build using Swift and referred as CoMPaS. The CoMPaS is available for iOS devices (iOS 9+).

INPUT DATA:

- the first ultrasound diagnostic data:
- date
 - diameter (mm)
- the second ultrasound diagnostic data:
 - date
 - diameter (mm)
- the number of affected lymph nodes (n)

OUTPUT DATA:

- the number of months
- category of forecast:
 - favorable
 - * mid-favorable
 - * unfavorable

To flesh this out, the Fig.3 provides a clinical example for a patient with seven affected lymph nodes.



Figure 3: Clinical example

Under such circumstances, it is necessary to collect predictions in one database to compare forecasts with real data and estimate effectiveness of proposed model. Consequently, the CoMPaS connects to database that allows us to test application and model.

As it turns out, the new predictive tool: 1) is a solid foundation to develop future studies of BC models; 2) does not require any expensive diagnostic tests; 3) is the first predictor that makes forecast using only current patient data, whilst the others are based on the additional statistical data.

Calculations of whole natural history resting on CoM-III

Given all above, it is relevant to dwell upon building the *whole* natural history of BC stage III. Provided formulas allow calculating:

- the number of doublings for secondary MTS relying only on two measurements of PT sizes;
- the correcting coefficient of secondary MTS spreading rate in patients with lymph nodes MTS relating with PT growth rate;
- doubling time of secondary MTS.

Data of a mean diameter of PT for each stage (T1, T2, T3, T4) is obtained from table 1 of paper J. Engel et al. [6]. The number of affected lymph nodes corresponds to TNM staging system of BC [21]. The variety of doubling time of PT (T1, T2, T3, T4) relying on PT sizes is calculated from fig 6 of paper D. Holzel et al. [9]. Table 2 shows results of calculations via CoM-III.

		T1a (mm) 1 < d ≤ 5	$\begin{array}{l} T1b \ (mm) \\ 5 < d \leq 10 \end{array}$	$\begin{array}{l} T1c \ (mm) \\ 10 < d \leq 20 \end{array}$	$\begin{array}{l} T2 \ (mm) \\ 20 < d \leq 50 \end{array}$	T3-4 (mm) d > 50	
1	Mean size of PT at surgery	4.5	8.5	15.1	28.5	64.6	[6]
2	pT_{log}	26.4	29.2	31.7	34.4	38.0	
3	$TVDT_{pT}$	80.0	75.0	70.0	65.0	60.0	[9]
4	Mean $K_{sMts(N-)}$ (N0, n=0)	1.00	1.00	1.00	1.00	1.00	
5	$TVDT_{sMts(N-)}$ (N0, n=0)	80.0	75.0	70.0	65.0	60.0	[23]
6	Mean $K_{sMts(N+)}$ (N1, $n_{mean}=2$)	1.23	1.16	1.12	1.09	1.05	
7	$TVDT_{sMts(N+)}$ (N1, $n_{mean}=2$)	65.09	64.44	62.37	59.77	56.90	[23]
8	Mean $K_{sMts(N+)}$ (N2, $n_{mean}=6$)	1.69	1.49	1.37	1.26	1.16	
9	$TVDT_{sMts(N+)}$ (N2, $n_{mean}=6$)	47.42	50.28	51.21	51.48	51.56	[23]
10	Mean $K_{sMts(N+)}$ (N3, n_{mean} =14)	2.60	2.15	1.86	1.61	1.38	
11	$TVDT_{sMts(N+)}$ (N3, n_{mean} =14)	30.74	34.93	37.71	40.30	43.42	[23]

Table 2: T1-3N0-3M0

Legend of Table 2:

- TNM parameters depend on PT size: T1, T2, T3, T4, N1, N2, N3, M0 [21] (see detailed description on Fig. 5 - Fig. 9);
- row 1 uses data of the mean sizes of PT at surgery from tables of paper [6];
- row 2 is calculated from row 1;
- row 3 uses data from figure of paper [9];
- *n_{mean}* is the mean number of lymph nodes whereas:
 - N1 means that the number of lymph nodes can equal any integer number from compact [1; 3];
 - N2 means that the number of lymph nodes can equal any integer number from compact [4; 9];
 - N3 means that the number of lymph nodes can equal any integer number from compact [10; 18];
 - N1-3 means that the number of lymph nodes can equal any integer number from compact [1; 18].
- $K_{sMts(N-)}$ means no MTS in lymph nodes (N0, $n_{mean}=0$);
- the variety of K_{sMts(N+)} is calculated for N1-3;
- the variety of $TVDT_{sMts(N+)}$ is calculated for N1-3.



Figure 4: T1aN0-3M0. Whole natural history of PT and secondary MTS of patients with lymph nodes MTS according to CoM-III. Parameter T (T1a: 1mm < d \leq 5mm) - diameter of PT. Parameter N (N0: n=0; N1: n=1-3; N2: n=4-9, N3: n=10-18) - affected lymph nodes.



Figure 5



Figure 6



Figure 7

Legend of Fig. 5-7:

red points blue points

correspond to PT growth; correspond to distant MTS growth;

- lines define boundaries of correcting coeffi-

nodes *n_{mean}*.

cients values for patients with N1, N2, N3; corresponds to the mean number of lymph

green line

64



Figure 8: T1bN0-3M0. Whole natural history of PT and secondary MTS of patients with lymph nodes MTS according to CoM-III. Parameter T (T1b: 5mm < d \leq 10mm) - diameter of PT. Parameter N (N0: n=0; N1: n=1-3; N2: n=4-9, N3: n=10-18) - affected lymph nodes.



Figure 9: T1cN0-3M0. Whole natural history of PT and secondary MTS of patients with lymph nodes MTS according to CoM-III. Parameter T (T1c: 10mm < d \leq 20mm) - diameter of PT. Parameter N (N0: n=0; N1: n=1-3; N2: n=4-9, N3: n=10-18) - affected lymph nodes.

4 CONCLUSION

The CoM-III model and predictive software: a) detect different growth periods of PT and secondary distant MTS growth in patients with lymph nodes MTS; b) make forecast of the period of secondary distant MTS appearance in patients with lymph nodes MTS; c) have higher average prediction accuracy than the other tools; d) can improve forecasts on survival of BC and facilitate optimisation of diagnostic tests. The following are calculated by CoM-III: the number of doublings for non-visible and visible growth periods of secondary distant MTS; tumor volume doubling time (days) for non-visible and visible growth periods of secondary distant MTS. The original CoM-III enables us, for the first time, to predict the whole natural history of PT and secondary distant MTS growth on each stage (T1, T2, T3, T4) for patients with/without lymph nodes MTS relying only on PT sizes. Summarising: CoM-III a) describes correctly PT and secondary distant MTS growth of T1N1M0, T2N1M0, T1-2N2M0, T3N1-2M0, T4N1-2M0, T1-4N3M0 [T1-4N1-3M0] stages in patients with lymph nodes MTS (N1-3); b) facilitates



Figure 10: T2N0-3M0. Whole natural history of PT and secondary MTS of patients with lymph nodes MTS according to CoM-III. Parameter T (T2: $20mm < d \le 50mm$) - diameter of PT. Parameter N (N0: n=0; N1: n=1-3; N2: n=4-9, N3: n=10-18) - affected lymph nodes.



Figure 11: T3N0-3M0. Whole natural history of PT and secondary MTS of patients with lymph nodes MTS according to CoM-III. Parameter T (T3: d > 50mm) - diameter of PT. Parameter N (N0: n=0; N1: n=1-3; N2: n=4-9, N3: n=10-18) - affected lymph nodes.

the understanding of the appearance period and inception of secondary distant MTS.

Work still to be done: 1. To test the CoM-III on clinical data. 2. To analyse forecasts statistically. 3. To implement CoM-III to medical practice.

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